

Show all work and circle/box your final answer. All answers must be simplified unless stated otherwise.

REVIEW (optional)

1. (0 points) Use intervals to describe the real numbers satisfying the following inequalities:

(a) $2 \leq x < 3$

(b) $x < 3$

2. (0 points) If $g(t) = t^3 - 3t^3 + t$, find $g(2)$ and $g(a)$

3. (0 points) Find the domain of the following functions

(a) $f(x) = \frac{3x - 5}{x^2 + x - 6}$

(b) $\sqrt{2x + 7} + \sqrt{x}$

4. (0 points) Let $f(x) = \begin{cases} \pi x^2 & , x < 2 \\ 1 + x & , 2 \leq x \leq 2.5 \\ 4x & , x > 2.5 \end{cases}$ Find $f(1)$, $f(2)$, and $f(3)$.

5. (0 points) Graph the following: $y = 3x + 1$ and $y = -2x + 3$.

6. (0 points) In 2010, a patient paid \$700 per day for a semiprivate hospital room and \$1900 for an appendectomy operation. Express the total amount paid for an appendectomy as a function of the number of days of hospital confinement.

7. (0 points) Express $\frac{x}{x-8} - \frac{x}{x-4}$ as a rational function.

8. (0 points) Factor the following:

(a) $x^2 + 8x + 15$

(b) $x^2 - 16$

(c) $3x^2 + 12x + 12$

(d) $3x - x^2$

9. (0 points) Simplify the following expressions:

(a) $\left(\frac{x^4}{y^2}\right)^3$

(b) $\frac{-x^3y}{-xy}$

(c) $8^{4/3}$

(d) $16^{1/2}$

10. (0 points) Find the equations of the lines satisfying the following properties:

(a) Slope is -1 ; $(7, 1)$ is on the line

(b) $(0, 0)$ and $(1, 0)$ is on the line

(c) Parallel to $y = 3x + 7$ and $(2, 0)$ is on the line

(d) Perpendicular to $y = -x$ and $(2, 0)$ is on the line

MAIN PROBLEMS

11. (0 points) Find the following limits:

(a) $\lim_{x \rightarrow 3} \sqrt{x^2 + 16}$

(d) $\lim_{x \rightarrow 6^-} \frac{|x - 6|}{x - 6}$

(b) $\lim_{x \rightarrow 0} \frac{x^2 + 3x}{x}$

(e) $\lim_{x \rightarrow 0} \frac{\sqrt{x^2 + 9} - 3}{x^2}$

(c) $\lim_{x \rightarrow 2} \frac{3x^2 - x - 10}{x^2 - 4}$

(f) $\lim_{x \rightarrow \infty} \frac{x^3 + 2x^2 + 1}{5x^5 + 4x^4 + 7}$

12. (0 points) Evaluate the following limits for $f(x)$

$$f(x) = \begin{cases} x^2 - 3x + 4 & x \leq 1 \\ x + 1 & 1 < x \leq 3 \\ x^2 - 3x + 4 & x > 3 \end{cases}$$

(a) $\lim_{x \rightarrow 1^-} f(x)$

(d) $\lim_{x \rightarrow 3^-} f(x)$

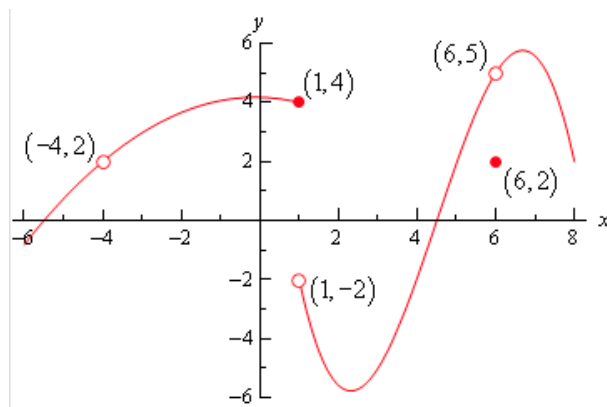
(b) $\lim_{x \rightarrow 1^+} f(x)$

(e) $\lim_{x \rightarrow 3^+} f(x)$

(c) $\lim_{x \rightarrow 1} f(x)$

(f) $\lim_{x \rightarrow 3} f(x)$

13. (0 points) Using the graph of $f(x)$ below, find the following limits:



(a) $\lim_{x \rightarrow 1^+} f(x)$

(b) $\lim_{x \rightarrow -4} f(x)$

(c) $\lim_{x \rightarrow 6} f(x)$