

Show all work and circle/box your final answer. All answers must be simplified unless stated otherwise.

1. (0 points) Let  $f(x, y, z) = 4x^4y^3z^2 - 3e^{2x}$ . Find  $\frac{\partial f}{\partial x}$ ,  $\frac{\partial f}{\partial y}$ , and  $\frac{\partial f}{\partial z}$ .
2. (0 points) Consider the function  $f(x, y) = x^2 + 2y^2 + 2xy + 2x + 4y + 7$ .
  - (a) Find the critical points of  $f(x, y)$ .
  - (b) Compute the number  $D(x, y)$ , and evaluate  $D$  at each critical point from part (a).
  - (c) Classify each critical point, using your answers to (a) and (b), as a maximum, minimum, saddle point, or that the test is inconclusive.
3. (0 points) Consider the function  $g(x, y) = -x^2 - y^2 + 3x - 2y$ .
  - (a) Find the critical points of  $g(x, y)$ .
  - (b) Compute the number  $D(x, y)$ , and evaluate  $D$  at each critical point from part (a).
  - (c) Classify each critical point, using your answers to (a) and (b), as a maximum, minimum, saddle point, or that the test is inconclusive.
4. (0 points) Let  $f(x, y) = x^2 + 4x - y^2 - 2y + 2$ 
  - (a) Find the critical points for  $f(x, y)$ .
  - (b) Use the second derivative test to determine whether the critical points from part (a) are maxima, minima, or saddles.
5. (0 points) Suppose you have the function of two variables  $f(x, y) = x^4 - 12x^2 - 4xy - y^2 + 16$ .
  - (a) Find the first partial derivatives  $\frac{\partial f}{\partial x}$  and  $\frac{\partial f}{\partial y}$
  - (b) Find all three second partial derivatives  $\frac{\partial^2 f}{\partial x^2}$ ,  $\frac{\partial^2 f}{\partial y^2}$ , and  $\frac{\partial^2 f}{\partial x \partial y}$
  - (c) Find and classify all critical points of the function using the second derivative test for functions of two variables.