

Show all work and circle/box your final answer. All answers must be simplified unless stated otherwise.

**1.** (0 points) Find the derivatives of the following functions

(a)  $\sqrt[3]{2x+1}$

(b)  $(4x+5)^2$

(c)  $24(4x+5)^5$

(d)  $(x^5+9)^3$

(e)  $(x^3+3)^4$

**2.** (0 points) Is the following function continuous at  $x = 1$ ? Is it differentiable at  $x = 1$ ?

$$f(x) = \begin{cases} \frac{2x-10}{4x^2+2} & x < 0 \\ 5 & 0 \leq x < 1 \\ \sqrt{x+24} & x \geq 1 \end{cases}$$

**3.** (0 points) Find the first and second derivative of the following functions:

(a)  $f(x) = -x^2 + 3$

(b)  $f(x) = \frac{x^3}{3} + \frac{x^2}{2} + \frac{x}{4}$

(c)  $r(\theta) = \frac{2}{\theta} - \frac{3}{\theta^3} + \frac{1}{\theta^4}$

**4.** (0 points) At time  $t$  seconds, the position of a body moving along the  $x$ -axis is  $s(t) = t^3 - 6t^2 + 9t$  meters.

(a) Find the body's acceleration each time the velocity is zero.

(b) Find the body's velocity each time the acceleration is zero.

**5.** (0 points) The revenue function for selling  $x$  units of a product is  $R(x) = 9x - 0.03x^2$ .

(a) Find the marginal revenue when production is at  $x = 10$  (Note: Marginal revenue is given by  $R'(x)$ )

(b) Estimate the revenue from selling  $x = 11$  units using your answer from part a.

**6.** (*0 points*) A company manufactures vinyl records for customers. They charge each customer \$5000 plus \$5.50 for each record manufactured. In terms of raw materials, it costs the company \$3.50 per record for materials and labor, plus \$15,000 for equipment and other costs.

(a) Find the Revenue, Cost, and Profit functions for this business.  
(Note: Profit=Revenue – Cost)

(b) What is the revenue, cost, and profit from producing 1000 records?