

Show all work and circle/box your final answer. All answers must be simplified unless stated otherwise.

1. (0 points) Find the following limits:

(a) $\lim_{x \rightarrow 0} \frac{\sin(4y)}{7y}$

(b) $\lim_{x \rightarrow \infty} \frac{x^2 + 8}{6x^2 - x}$

(c) $\lim_{x \rightarrow \infty} \frac{5x^3 + 7x - 8}{-4x^2 - 2x + 1}$

(d) $\lim_{x \rightarrow \infty} \frac{x^2 - 5x - 9}{2x^4 + 3x^3}$

(e) $\lim_{t \rightarrow 2^-} \frac{t + 2}{t - 2}$

2. (0 points) Find $\lim_{x^2-4} \frac{1}{x^2-4}$ as

(a) $x \rightarrow 2^+$

(b) $x \rightarrow 2^-$

(c) $x \rightarrow -2^+$

(d) $x \rightarrow -2^-$

3. (*0 points*) It can be shown that the inequalities

$$1 - \frac{x^2}{6} < \frac{x \sin x}{2 - 2 \cos x} < 1$$

hold for all values of x close to zero. What, if anything, does this tell you about

$$\lim_{x \rightarrow 0} \frac{x \sin x}{2 - 2 \cos x}?$$

Give reasons for your answer.

4. (*0 points*) Use the squeeze theorem to find $\lim_{x \rightarrow \infty} \frac{\sin 3x}{x}$.

5. (0 points) Is the following function continuous at $x = 0$?

$$f(x) = \begin{cases} \frac{x-6}{x-3} & x < 0 \\ 2 & x = 0 \\ \sqrt{4+x^2} & x > 0 \end{cases}$$