

Show all work and circle/box your final answer. All answers must be simplified unless stated otherwise.

1. Find the following limits:

(a) $\lim_{x \rightarrow 3} \sqrt{x^2 + 16}$

(b) $\lim_{x \rightarrow 0} \frac{x^2 + 3x}{x}$

(c) $\lim_{x \rightarrow 2} \frac{3x^2 - x - 10}{x^2 - 4}$

(d) $\lim_{x \rightarrow \infty} \frac{x^3 + 2x^2 + 1}{5x^5 + 4x^4 + 7}$

2. Evaluate the following limits for $f(x)$

$$f(x) = \begin{cases} x^2 - 3x + 4 & x \leq 1 \\ x + 1 & 1 < x \leq 3 \\ x^2 - 3x + 4 & x > 3 \end{cases}$$

(a) $\lim_{x \rightarrow 1^-} f(x)$

(d) $\lim_{x \rightarrow 3^-} f(x)$

(b) $\lim_{x \rightarrow 1^+} f(x)$

(e) $\lim_{x \rightarrow 3^+} f(x)$

(c) $\lim_{x \rightarrow 1} f(x)$

(f) $\lim_{x \rightarrow 3} f(x)$

3. Is the following function continuous at $x = 1$? $x = 0$?

$$f(x) = \begin{cases} \frac{2x-10}{4x^2+2} & x < 0 \\ 5 & 0 \leq x < 1 \\ \sqrt{x+24} & x \geq 1 \end{cases}$$