

Show all work and circle/box your final answer. All answers must be simplified unless stated otherwise.

- (1) Consider the function $f(x, y) = x^2 + 2y^2 + 2xy + 2x + 4y + 7$.
 - (a) Find the critical points of $f(x, y)$.
 - (b) Compute the number $D(x, y)$, and evaluate D at each critical point from part (a).
 - (c) Classify each critical point, using your answers to (a) and (b), as a maximum, minimum, saddle point, or that the test is inconclusive.

- (2) Consider the function $g(x, y) = -x^2 - y^2 + 3x - 2y$.
 - (a) Find the critical points of $g(x, y)$.
 - (b) Compute the number $D(x, y)$, and evaluate D at each critical point from part (a).
 - (c) Classify each critical point, using your answers to (a) and (b), as a maximum, minimum, saddle point, or that the test is inconclusive.

- (3) Let $f(x, y) = x^2 + 4x - y^2 - 2y + 2$
 - (a) Find the critical points for $f(x, y)$.
 - (b) Use the second derivative test to determine whether the critical points from part (a) are maxima, minima, or saddles.

- (4) Suppose you have the function of two variables $f(x, y) = x^4 - 12x^2 - 4xy - y^2 + 16$.
 - (a) Find the first partial derivatives $\frac{\partial f}{\partial x}$ and $\frac{\partial f}{\partial y}$
 - (b) Find all three second partial derivatives $\frac{\partial^2 f}{\partial x^2}$, $\frac{\partial^2 f}{\partial y^2}$, and $\frac{\partial^2 f}{\partial x \partial y}$
 - (c) Find and classify all critical points of the function using the second derivative test for functions of two variables.