

Show all work and circle/box your final answer. All answers must be simplified unless stated otherwise.

1. Find the absolute extrema of  $f(x) = 3x^4 - 4x^3$  on the interval  $[-1, 2]$
2. Find the absolute maximum and minimum values of the function  $f(x) = \frac{x}{(2x+1)^2}$  on  $0 \leq x \leq 2$
3. Find all values of  $c$  that satisfy the conclusion of the mean value theorem for the function  $f(x) = x^2 - 5x + 4$  on the interval  $[1, 4]$
4. Show that  $x^5 + 10x + 3 = 0$  has exactly one solution.
5. Show that  $f(x) = x^4 + 3x + 1$  has exactly one zero in the interval  $[-2, -1]$