Math 241 Spring 2019 Professor MG Classwork 9

Name: \_\_\_\_\_

Show all work and circle/box your final answer. All answers must be simplified unless stated otherwise.

- 1. Approximate the area under the graph of  $f(x) = x^2$  and above the x-axis from x = 1 to x = 5 using the following methods with n = 4. (a) Use left endpoints. (b) Use right endpoints. (c) Average the answers in parts a and b. (d) Use midpoints.
- 2. Suppose that f and h are integrable and that

$$\int_{1}^{9} f(x) \, dx = -1, \ \int_{7}^{9} f(x) \, dx = 5, \ \int_{7}^{9} h(x) \, dx = 4$$

Find

(a) 
$$\int_{9}^{7} [h(x) - f(x)] dx$$
  
(b)  $\int_{7}^{9} [2f(x) - 3h(x)] dx$   
(c)  $\int_{1}^{7} f(x) dx$ 

3. Evaluate the following integrals:

(a) 
$$\int_{1}^{2} \frac{4t^{2} + 2t^{3} + 8}{4t^{2}} dt$$
  
(b)  $\int_{-2}^{2} (x^{3} - 2x + 3) dx$   
(c)  $\int_{1/2}^{3/2} (-2x + 4) dx$  (Check your answer using area)

- 4. Find  $\frac{d}{dx} \int_{1}^{\sin x} 3t^2 dt$  by
  - (a) By evaluating the integral and differentiating the result
  - (b) By differentiating the integral directly (i.e. using FTC part 1).