

Conditional Probability

The probability of an event occurring, given that another event has already occurred

P(B|A) means "the probability of B, given A"

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Some Examples

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You choose two cards from a deck.

What is the probability that the second card you chose is a queen given that the first was a king (and you didn't put the king back in)? You have 5 marbles, 2 are blue and 3 are red

If A is the event that you select a red marble and B is the event that you select a blue marble, find P(A|B) and P(B|A).



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Example

You are studying the effect of a certain gene on an individual's IQ. You collect the data summarized on the right.

- Find the probability that a person has a high IQ, given that they have the gene.
- 2. Find the probability that a person does not have the gene.
- Find the probability that a person does not have the gene, given that they have a normal IQ.

	Has Gene	Doesn't have gene	Total
High IQ	33	19	52
Normal IQ	39	11	50
Total	72	30	102

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Independent Events

Two events are independent when the occurrence of one event does not affect the probability of the occurrence of the other.

In other words, P(B|A)=P(B) or P(A|B)=P(A)

For example: Flipping a coin two times. The second coin flip is independent from the first.

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Example: Dependent VS. Independent

Selecting a king from a deck and then selecting a queen (without replacement)

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Dependent



Independent

Tossing a coin and getting heads then rolling a six-sided die and getting 6









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You select two cards (without replacement). Find the probability that you pick a king and a queen.

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You flip a coin and roll a 6-sided die. Find the probability that you get a head and a 6.

 $rac{1}{6}pprox 0.083$

 $\frac{1}{2}$.

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 $rac{4}{52}\cdotrac{4}{51}pprox 0.006$

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c) 1-0.0001 = 0.9999

b) (0.05)(0.05)(0.05) ≈ 0.0001

a) (0.95)(0.95)(0.95) ≈ 0.857

Example: The probability of a reconstructive ACL surgery being successful is 95%. Find the following:
a) The probability that 3 surgeries are successful
b) The probability that none of them are successful
c) The probability that at least one of them is successful



