



# CHAPTER 4

## DISCRETE PROBABILITY DISTRIBUTIONS

ACSTA101 - Professor MG





MENU

ANALYSIS

CONTACT

DATA ANALYSIS



# PROBABILITY DISTRIBUTIONS





# THERE ARE TWO TYPES OF RANDOM VARIABLES



## DISCRETE

Possible outcomes are finite or countable. Can only take on very specific values.

VS

## CONTINUOUS

Has an uncountable number of possible outcomes. Can take on any value in an interval.





# EXAMPLES



## DISCRETE

The number of calls a salesperson makes in a day

## DISCRETE

The number of Arrupe students who are pre-majoring in business

## DISCRETE

The value you get when rolling a 6-sided die

## CONTINUOUS

The amount of time spent on your phone in a day

## CONTINUOUS

The volume of gas in a 21-gallon tank

## CONTINUOUS

The height of an individual person





Definition: A discrete probability distribution lists each possible value together with its probability. It must satisfy the following:

1.  $0 \leq P(X) \leq 1$
2.  $\sum P(X) = 1$





# CONSTRUCTING A DISCRETE PROBABILITY DISTRIBUTION

Let  $x$  be a discrete random variable with possible outcomes

$x_1, x_2, \dots, x_n$

- Make a frequency distribution for the possible outcomes.
- Find the sum of the frequencies.
- Find the probability of each possible outcome by dividing its frequency by the sum of the frequencies.
- You can also modify the stroke, its color, thickness or type
- Check that each probability is between 0 and 1 and that the sum is 1.





# EXAMPLE

Score (x)	Freq (f)
1	24
2	33
3	42
4	30
5	21

An industrial psychologist administered a personality inventory test for passive aggressive traits to 150 employees. Individuals were given a score from 1 to 5, where 1 was extremely passive and 5 was extremely aggressive. A score of 3 indicated neither trait. Construct a probability distribution for the random variable  $x$ . Then graph the distribution using a histogram.

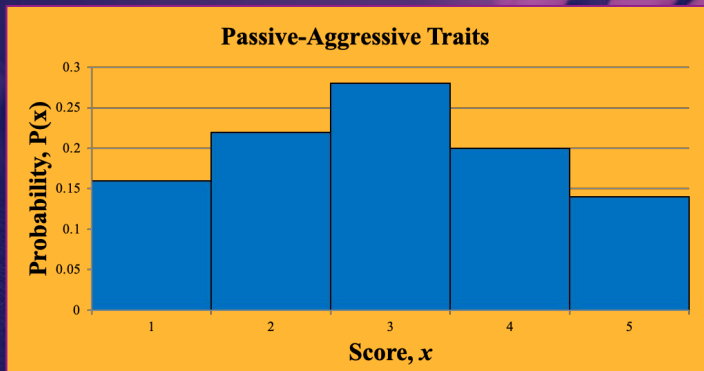




# EXAMPLE CONTINUED

<b>x</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>
<b>P(x)</b>	<b>0.16</b>	<b>0.22</b>	<b>0.28</b>	<b>0.20</b>	<b>0.14</b>

○



## Examples of interpreting this data:

- The probability that a person scored 4 is 20%
- The probability that a person scored at least 3 is 62%







# MEAN, VARIANCE, AND STANDARD DEVIATION



MEAN

$$\mu = \sum xP(x)$$



VARIANCE

$$\sigma^2 = \sum (x - \mu)^2 P(x)$$



STANDARD DEVIATION

$$\sigma = \sqrt{\sum (x - \mu)^2 P(x)}$$





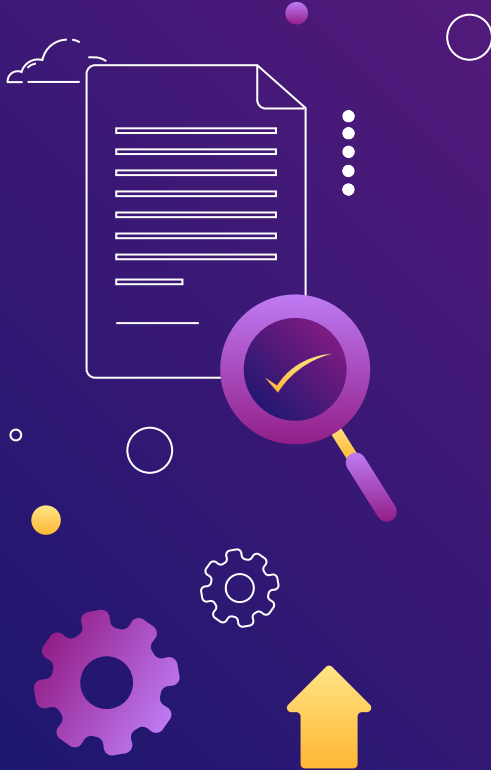
# EXAMPLE CONT.

$$\mu = 1(0.16) + 2(0.22) + \dots + 5(0.14) \approx 2.9$$

$$\sigma^2 = (1 - 2.9)^2(0.16) + \dots + (5 - 2.9)^2(0.14) \approx 1.6164$$

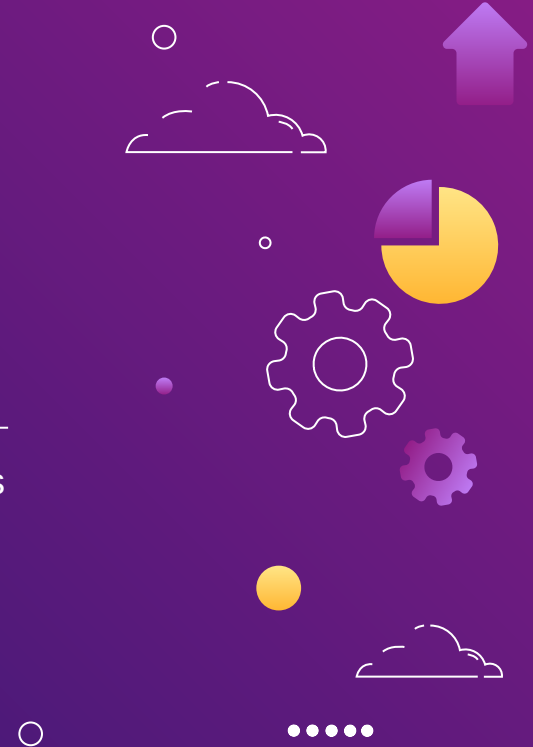
$$\sigma = \sqrt{1.6164} \approx 1.3$$





# EXPECTED VALUE

The expected value of a variable is equal to the mean. It is what you would expect the variable to tend towards in the long run





# EXAMPLE

At a raffle, 1500 tickets are sold at \$2 each for four prizes of \$500, \$250, \$150, and \$75. You buy one ticket. What is the expected value of your gain?

Gain	\$498	\$248	\$148	\$73	\$-2
P(x)	1/1500	1/1500	1/1500	1/1500	1496/1500

$$\begin{aligned} E(x) &= 498 \left( \frac{1}{1500} \right) + \dots + (-2) \left( \frac{1496}{1500} \right) \\ &= \$ - 1.35 \end{aligned}$$

