

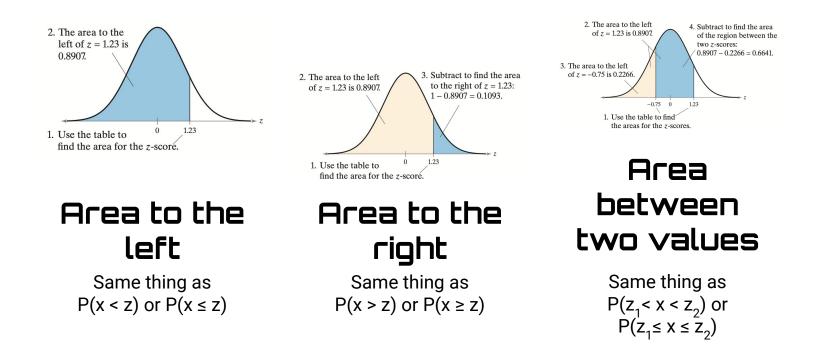


Finding the probability that *x* lies in a given interval of a normal distribution is the same thing as finding the area under the curve of that interval.

Steps:

- 1. Convert the boundaries to a z-score
- 2. Determine which corresponding area under the curve you're looking for
- 3. Use a standard table or your calculator to find the area

Probability and Area



Example: A survey indicates that for each trip to the supermarket, a shopper spends an average of 45 minutes with a standard deviation of 12 minutes in the store. The length of time spent in the store is normally distributed and is represented by the variable x. A shopper enters the store. Find:
a) The probability that the shopper spends between

22 and 52 min

b) The probability that the shopper spends more than 37 min

Example: A survey indicates that people use their cellular phones an average of 1.5 years before buying a new one. The standard deviation is 0.25 year. A cellular phone user is selected at random. Find the probability that the user will use their current phone for less than 1 year before buying a new one. Assume that the variable x is normally distributed.

Normal Distributions: Finding Values



In the previous sections, you were given a value and asked to find an area/probability. But what if you had to do the opposite?

Steps to find a value given a probability:

Find the corresponding z-score

You can do this by looking at the closest value on a standard table and finding the z-score associated to that entry, or using technology

Convert the z-score to a value

Equation for this: $x = \mu + z\sigma$

Practicing Step 1:

Find the z-score that corresponds to a cumulative area of 0.3632.

Find the z-score that has 10.75% of the distribution's area to its right.

Find the z-scores for which 68% of the distribution's area lies between -z and z

Practicing Step 2:

A veterinarian records the weights of cats treated at a clinic. The weights are normally distributed, with a mean of 9 pounds and a standard deviation of 2 pounds. Find the weight x corresponding to each z-score below. Interpret the results.

Putting them together:

Example: Scores for the California Peace Officer Standards and Training test are normally distributed, with a mean of 50 and a standard deviation of 10. An agency will only hire applicants with scores in the top 10%. What is the lowest score you can earn and still be eligible to be hired by the agency?

Answer key:

Curve A has the greater mean, Curve Ex 1 (two curves) B has the greater standard deviation Ex 2 (cumul. areas) 0.8749, 0.4052, and 0.1611 Ex 3 (other areas) 0.1446 and 0.8275 Ex 4 (shop survey) 0.7333 and 0.6915 Ex 5 (cell phones) 0.0228 Ex 6 (step 1) -0.35, 1.24, and 0.9945

Answer key continued:Ex l(step 2)12.92 lbs, 8.12 lbs, and 9 lbsEx 8 (peace officer)62.8